



GEOMIX

Geometric methods for non-linear spectral unmixing

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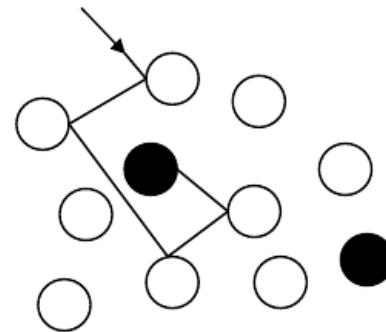
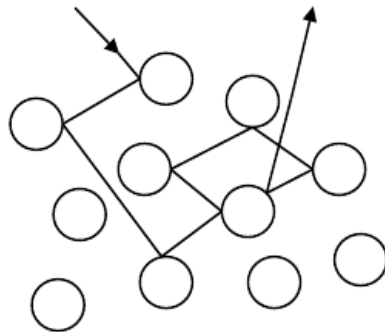
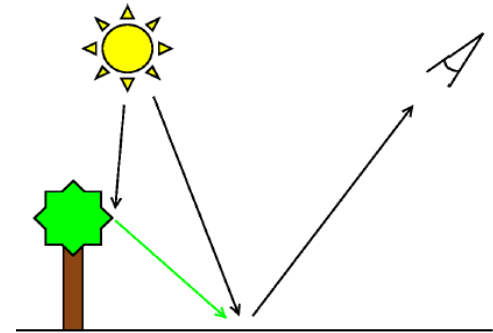
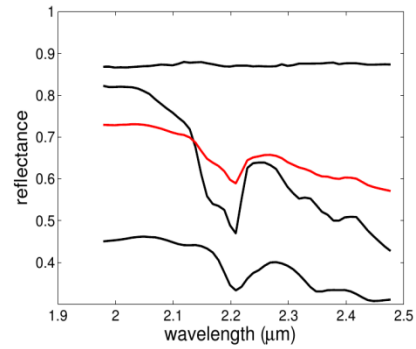
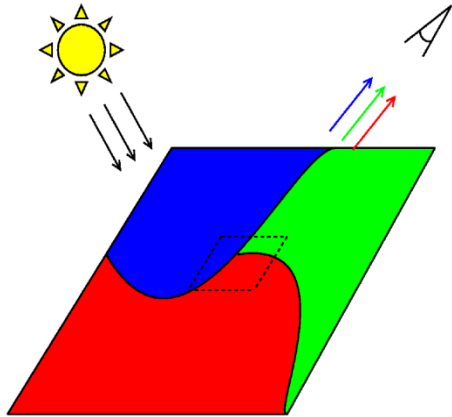
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BEODAY November 24, 2020

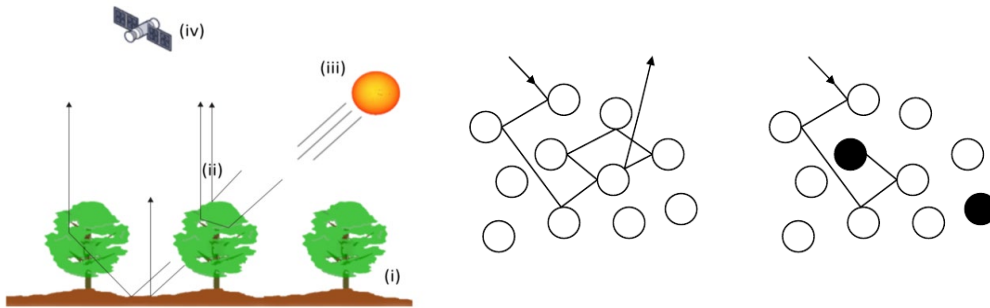


General context: Nonlinear Spectral mixing

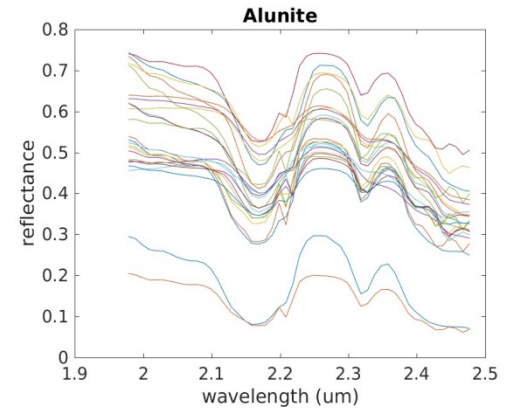


Specific goals

Nonlinear effects



Spectral variability



Validation

1. A physics-based nonlinear model

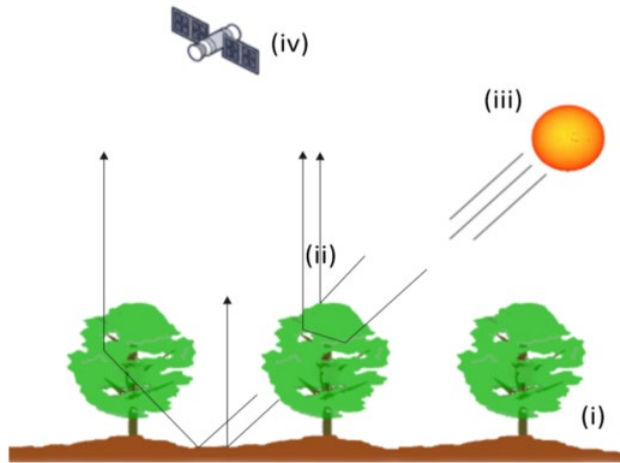
- Easy to use:
 - Model easy to invert and fit to data
 - Parameters have clear physical meaning
- Allows to include shadows, skylight, neighbor effect

2. A data driven method nonlinear unmixing framework

- Flexible, independent of specific model
- Supervised approach (ground truth training and validation data)
- Accounts for spectral variability

1. Multilinear mixing model

Parameter P for multiple reflections



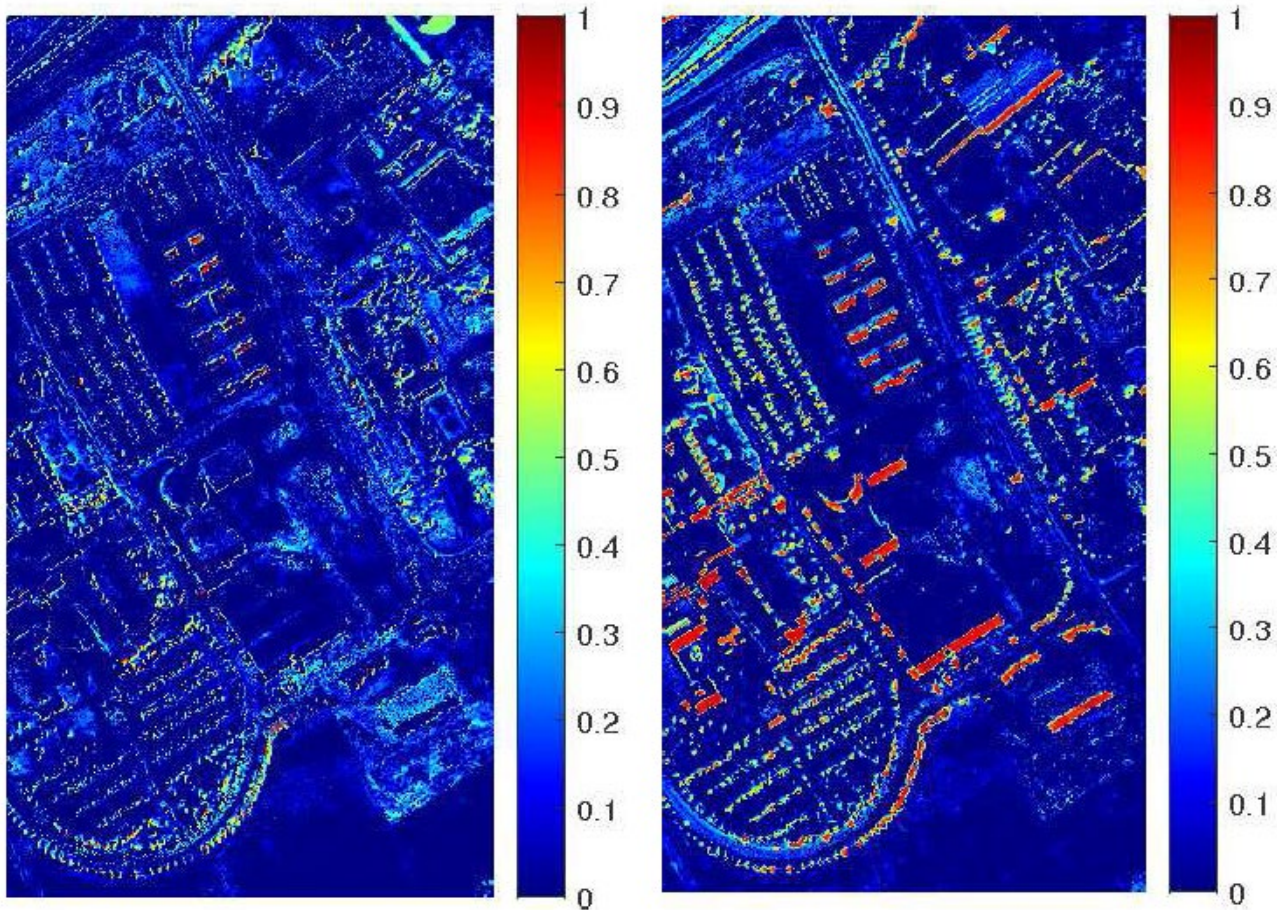
Parameter Q for shadow



$$\begin{aligned}
 &= (1 - P) \sum_{i=1}^p a_i \mathbf{e}_i + (1 - P)P \sum_{i=1}^p \sum_{j=1}^p a_i a_j \mathbf{e}_i \odot \mathbf{e}_j \\
 &+ (1 - P)P^2 \sum_{i=1}^p \sum_{j=1}^p \sum_{k=1}^p a_i a_j a_k \mathbf{e}_i \odot \mathbf{e}_j \odot \mathbf{e}_k \dots \\
 &= \frac{(1 - P) \sum_{i=1}^p a_i \mathbf{e}_i}{1 - P \sum_{i=1}^p a_i \mathbf{e}_i}
 \end{aligned}$$

$$- Q(1 - P) \sum_{i=1}^p a_i \mathbf{e}_i$$

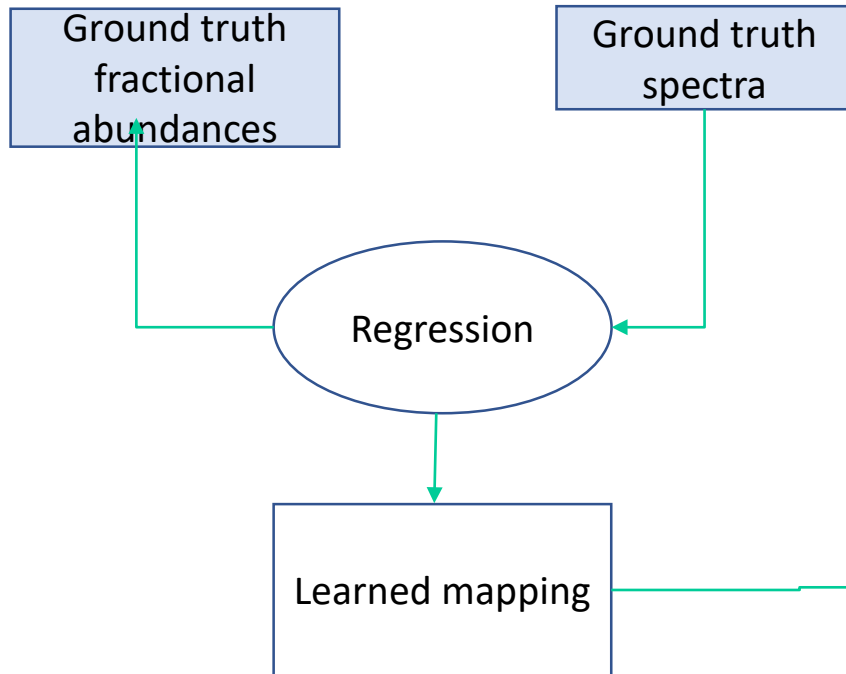
1. Multilinear mixing model



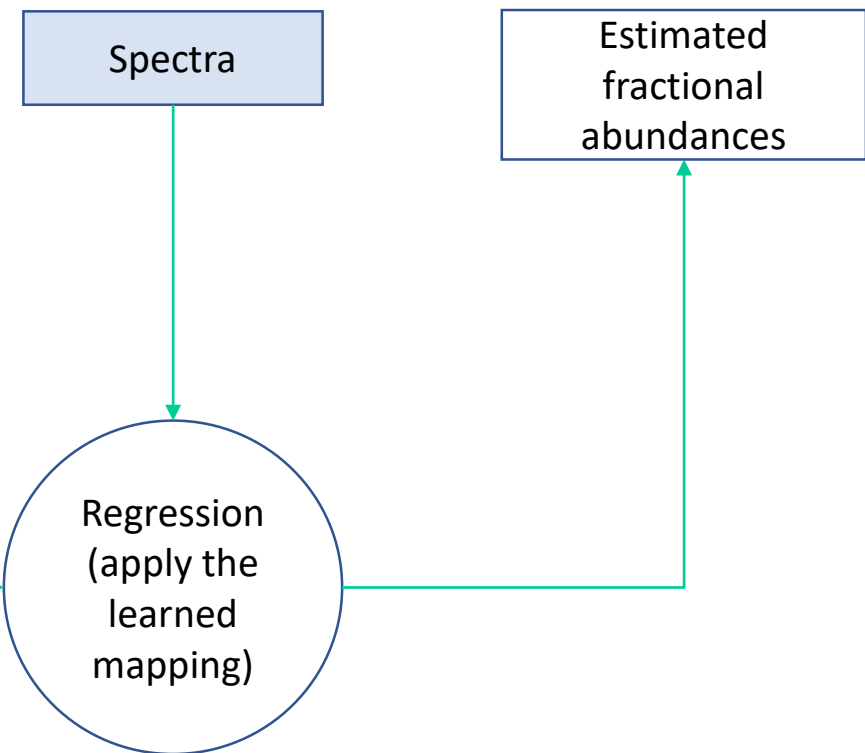
R. Heylen, V. Andrejchenko, Z. Zahiri, M. Parente, P. Scheunders. Nonlinear hyperspectral unmixing with graphical models. *IEEE Transactions on Geoscience and Remote Sensing*, 57 (7), 4844-4856, 2019.

2. Supervised nonlinear unmixing framework

TRAINING

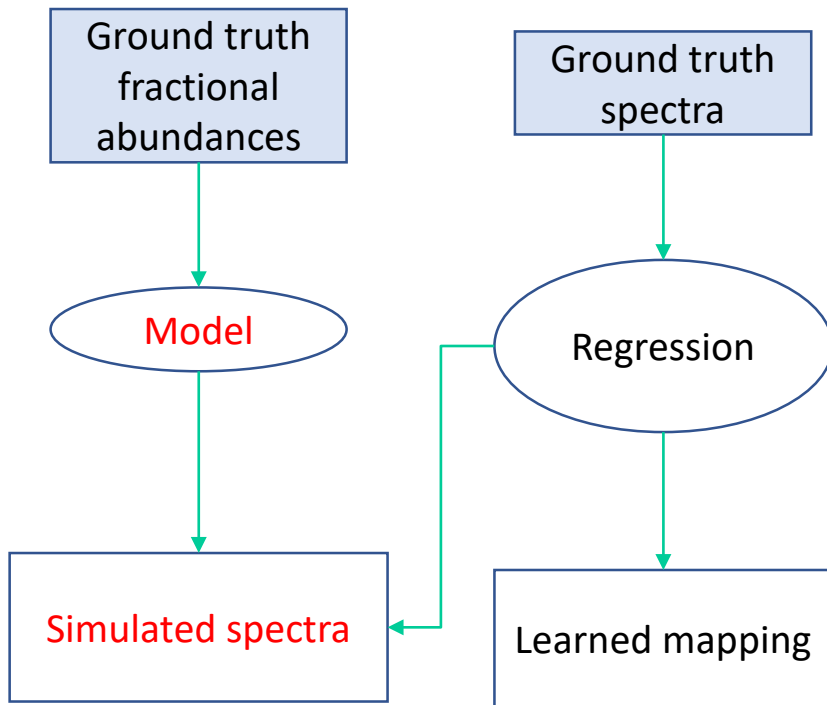


VALIDATION

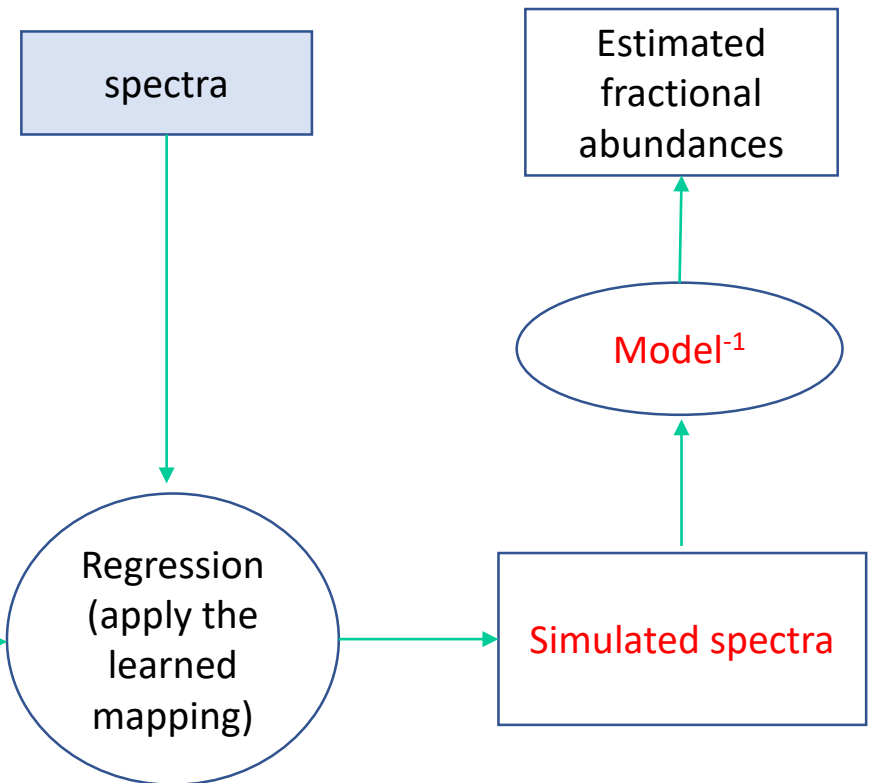


2. Supervised nonlinear unmixing framework

TRAINING



VALIDATION



2. Supervised nonlinear unmixing framework

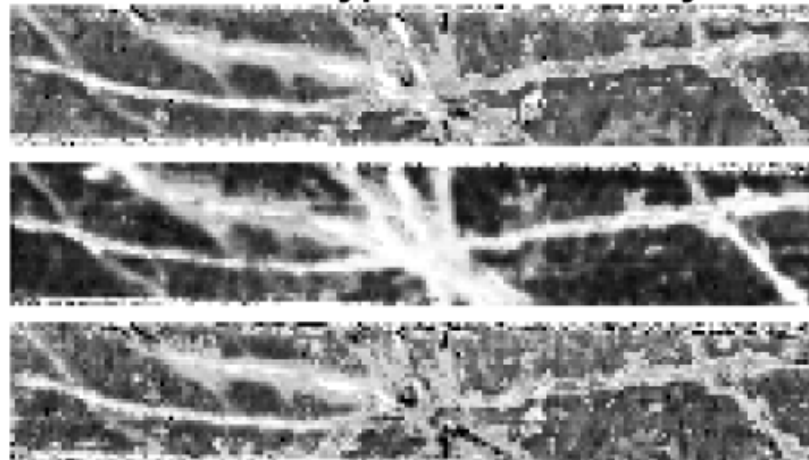
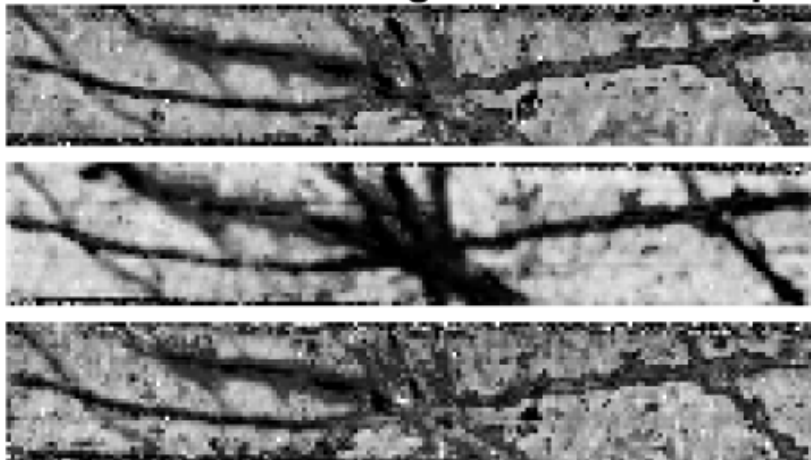


Collaboration with Helmholtz-Zentrum Dresden-Rossendorf (HZDR), Helmholtz Institute Freiberg for Resource Technology (HIF), Germany

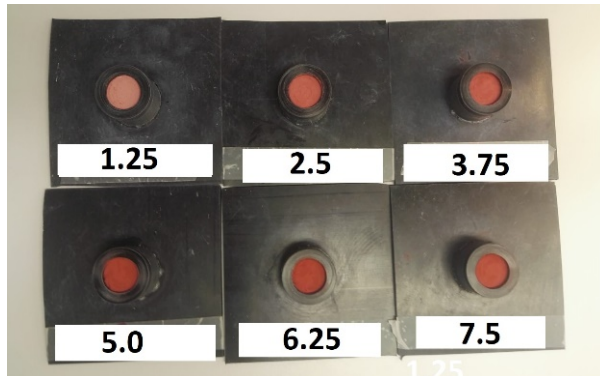
Biotite+Chlorite+Plagioclase+K-Feldspar

White Mica+Gypsum+Quartz+Pyrite

GP_LM
NN_LM
KRR_LM



2. Supervised nonlinear unmixing framework



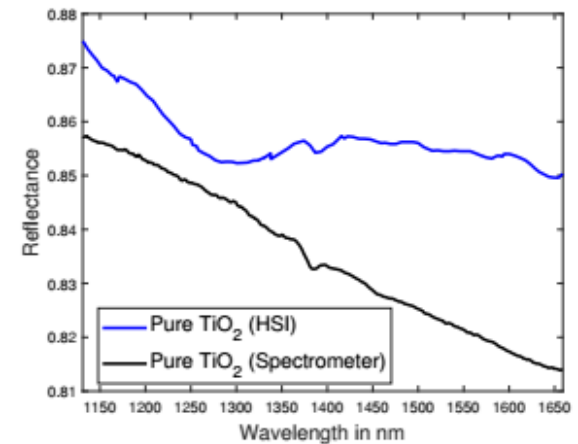
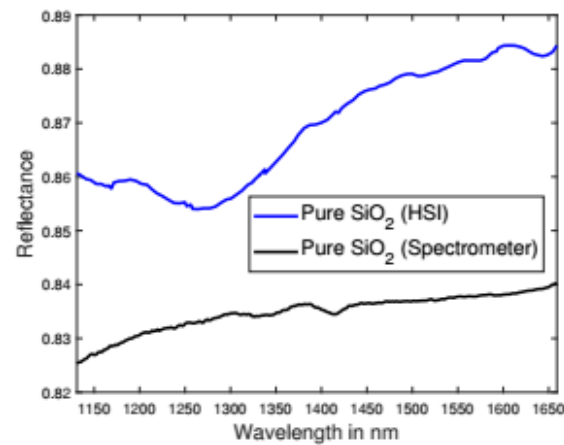
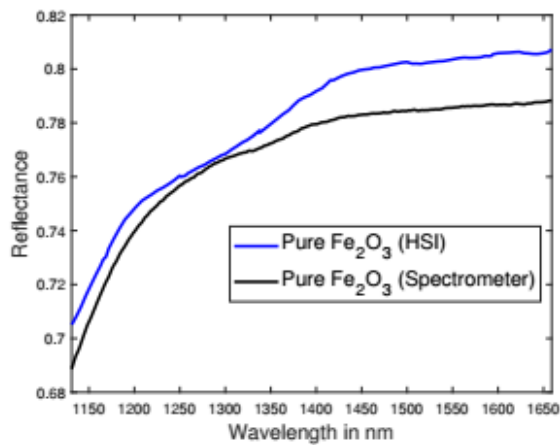
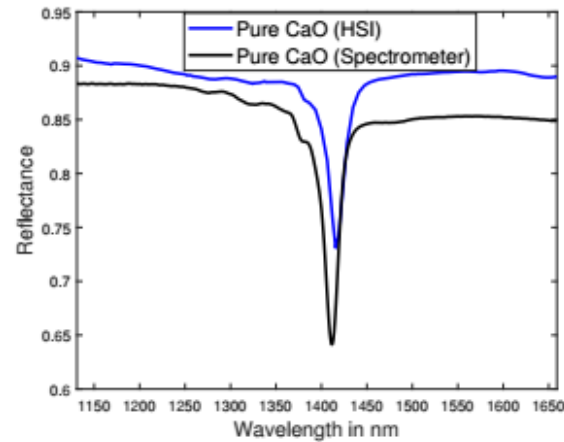
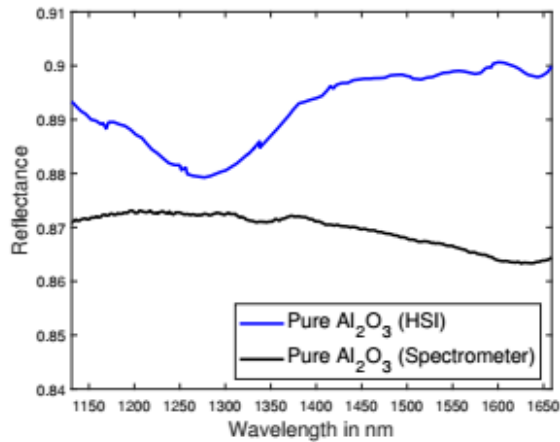
Pure Mineral	Density (g/cm ³)	Grain size (μm)
Fe ₂ O ₃	5.25	0.8
Al ₂ O ₃	3.98	3.5
SiO ₂	2.64	23
TiO ₂	3.89	0.5
CaO	3.34	2.7

Mineral powder mixtures



Different binary mixtures	
Endmember 1	Endmember 2
Al ₂ O ₃	SiO ₂
CaO	SiO ₂
CaO	TiO ₂
Fe ₂ O ₃	Al ₂ O ₃
Fe ₂ O ₃	CaO
Fe ₂ O ₃	SiO ₂
SiO ₂	TiO ₂

2. Supervised nonlinear unmixing framework



Mineral powder mixtures

2. Supervised nonlinear unmixing framework

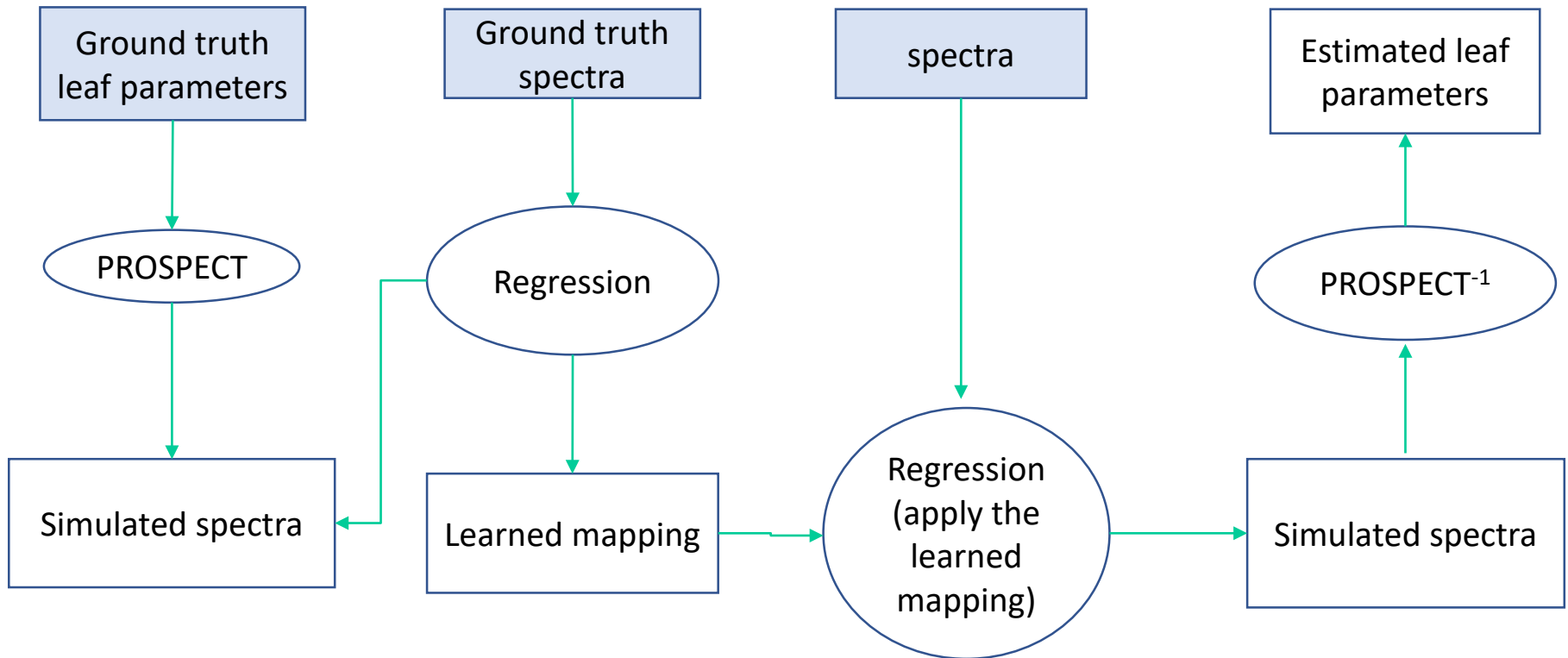
Conclusions

- Mixing models completely fail (even Hapke model): not robust to spectral variability.
- Data-driven approaches fail, physical relation between the spectra and the fractional abundances is lost.
- The proposed hybrid approach: error rates of only a few percent.

2. Supervised nonlinear unmixing framework

TRAINING

VALIDATION



Future activities 2020-2021

Fundamental research a real quantitative approach

- Understand spectral variability
- Reduce dependence on training data

Damage detection for Industrial application

- Mixtures of active minerals and water
- Corrosion
- Concrete damages
- Coating problems
- ...

Remote sensing applications

- crop leaf parameter estimation from remote sensing time series